



3.17H Transformations: Higher Tier Practice

EDEXCEL Edexcel 1MA1 · Calculator allowed · about 75 minutes

Total Marks

Name: _____ Date: ____ / ____ / ____

Answer ALL questions. Show all your working.

- 1** Triangle A has vertices A(1, 2), B(4, 2) and C(1, 5). Describe fully the single transformation that maps triangle A to triangle A' with vertices A'(1, -2), B'(4, -2) and C'(1, -5).

(Total for Question 1 is 2 marks)

- 2** Enlarge triangle T with vertices (2, 1), (4, 1) and (2, 3) by a scale factor of -2 centre (1, 1). Find the coordinates of the image vertices.

(Total for Question 2 is 3 marks)

- 3** A transformation maps the point P(3, -1) first by a shear in the x-direction with shear factor 2 (so $(x, y) \rightarrow (x + 2y, y)$), then by a rotation of 90 degrees anticlockwise about the origin. Find the final coordinates of P after both transformations.

(Total for Question 3 is 4 marks)

- 4 Triangle DEF is translated by vector $\mathbf{v}$ to triangle D'E'F'. Point D does not move under the translation. If D has coordinates (2, 3), state the translation vector $\mathbf{v}$ and explain what this implies about D'E'F'.

(Total for Question 4 is 3 marks)

- 5 The transformation T maps the vector $\mathbf{a} = (3, 2)$ to $\mathbf{a}' = (6, 4)$. It maps $\mathbf{b} = (1, -1)$ to $\mathbf{b}' = (2, -2)$. Write down the single transformation T and explain briefly how you know. State the image of $\mathbf{c} = (5, 0)$ under T.

(Total for Question 5 is 4 marks)

- 6 Show that the composite transformation consisting of a rotation of 180 degrees about the origin followed by a reflection in the line $y = -x$ maps any point (x, y) to (y, x) . Explain each step.

(Total for Question 6 is 5 marks)

- 7 A right-angled triangle with vertices P(0, 0), Q(6, 0) and R(6, 8) is transformed by a clockwise rotation of 90 degrees about the point (6, 0), then translated by vector $(-4, 2)$. Find the coordinates of the image of R after the two transformations.

(Total for Question 7 is 4 marks)

- 8** The matrix $M = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$ acts on column vectors $(x, y)^T$. (a) Identify the single transformation represented by M . (b) Use M to find the image of the point $S(2, -3)$.

(a) (a) Identify the single transformation represented by M . (2)

(b) (b) Use M to find the image of the point $S(2, -3)$. (3)

(Total for Question 8 is 5 marks)

- 9** A regular pentagon has centre O and a vertex at $V(0, r)$ on the positive y -axis. A rotation of 72 degrees anticlockwise about O maps the pentagon to itself, sending V to the next vertex W . Express the rotation as a 2×2 matrix R in terms of $\cos(72 \text{ degrees})$ and $\sin(72 \text{ degrees})$. Then show that applying R to V gives the coordinates of W in terms of r , $\cos(72 \text{ degrees})$ and $\sin(72 \text{ degrees})$.

(a) Write down the 2×2 matrix R representing a rotation by 72 degrees anticlockwise about the origin. (2)

(b) Use R to find the coordinates of W , the image of $V(0, r)$, in terms of r , $\cos 72$ and $\sin 72$. (3)

(Total for Question 9 is 5 marks)

Mark scheme · 3.17H Transformations: Higher Tier Practice

Question 1

- **B1** state reflection in the x-axis oe
- **B1** fully described mapping $(x, y) \rightarrow (x, -y)$ or equivalent cao
- **Answer: Reflection in the x-axis. $(x, y) \rightarrow (x, -y)$.**

Question 2

- **M1** subtract centre (1,1) then multiply by -2 for each coordinate (method shown) oe
- **A1** image of (2,1) is (-1,1) cao
- **A1** images of other vertices: $(4,1) \rightarrow (-5,1)$ and $(2,3) \rightarrow (-1,-3)$ cao
- **Answer: Images: $(2,1) \rightarrow (-1,1)$; $(4,1) \rightarrow (-5,1)$; $(2,3) \rightarrow (-1,-3)$.**

Question 3

- **M1** apply shear: $(3, -1) \rightarrow (3 + 2(-1), -1) = (1, -1)$ or equivalent method
- **M1** apply rotation 90 anticlockwise about origin: $(x, y) \rightarrow (-y, x)$ applied to (1, -1)
- **A1** state intermediate result $(-y, x) = (-(-1), 1) = (1, 1)$ cao
- **B1** final coordinates clearly stated as (1, 1) cao
- **Answer: Final coordinates: (1, 1).**

Question 4

- **B1** state vector $v = (0, 0)$ or 'no translation' oe
- **B1** state $D' = D$ or give coordinates $D' = (2, 3)$ cao
- **B1** conclude D'E'F' coincides with DEF (the whole triangle is unchanged) oe
- **Answer: Translation vector $v = (0, 0)$. $D' = D = (2, 3)$, so D'E'F' coincides with DEF (no change).**

Question 5

- **M1** identify common multiplication by 2 for given vectors or state scale factor 2
- **A1** state transformation is enlargement with scale factor 2 centre at origin (or equivalent) cao
- **M1** apply to c: $(5,0) \rightarrow (10,0)$
- **A1** state image (10, 0) cao
- **Answer: T is an enlargement with scale factor 2 centre at the origin. Image of c is (10, 0).**

Question 6

- **M1** state rotation 180 about origin maps $(x, y) \rightarrow (-x, -y)$ or show this algebraically
- **M1** state reflection in $y = -x$ maps $(u, v) \rightarrow (-v, -u)$
- **M1** apply to $(-x, -y)$: substitute $u = -x$, $v = -y$ to get $(-v, -u)$
- **M1** simplify $(-v, -u) = (-(-y), -(-x)) = (y, x)$
- **A1** conclude with clear explanation linking combined steps to obtain (y, x) (final statement) cao
- **Answer: Rotation 180: $(x, y) \rightarrow (-x, -y)$. Reflection in $y = -x$: $(u, v) \rightarrow (-v, -u)$. Apply: $(-x, -y) \rightarrow (y, x)$. Hence the composite transformation maps (x, y) to (y, x) .**

Question 7

- **M1** apply rotation 90 clockwise about (6,0): translate so centre at origin then rotate, method shown
- **M1** compute position after rotation: R(6,8) relative to centre (6,0) is (0,8) $\rightarrow$ rotate 90 clockwise to (8,0) then translate back to (14,0) oe
- **M1** apply translation $(-4,2)$ to (14,0) gives (10,2) oe
- **A1** final coordinates (10, 2) cao
- **Answer: Image of R is (10, 2).**

Question 8

- (a) **B1** state rotation of 90 degrees anticlockwise about the origin oe
- (a) **B1** reference to mapping rule or effect on axes (e.g. $(1,0) \rightarrow (0,1)$) cao
- (a) **Answer: Rotation 90 degrees anticlockwise about the origin.**
- (b) **M1** multiply matrix by vector: show calculation $\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} * (2, -3)^T$
- (b) **M1** compute entries: first entry $0*2 + (-1)*(-3) = 3$, second entry $1*2 + 0*(-3) = 2$
- (b) **A1** state image $(3, 2)$ cao
- (b) **Answer: $(3, 2)$**

Question 9

- (a) **M1** state general rotation matrix form $\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$ oe
- (a) **A1** substitute $\theta = 72$ degrees: $R = \begin{bmatrix} \cos 72 & -\sin 72 \\ \sin 72 & \cos 72 \end{bmatrix}$ cao
- (a) **Answer: $R = \begin{bmatrix} \cos 72 & -\sin 72 \\ \sin 72 & \cos 72 \end{bmatrix}$**
- (b) **M1** multiply matrix by vector: show $\begin{bmatrix} \cos 72 & -\sin 72 \\ \sin 72 & \cos 72 \end{bmatrix} * (0, r)^T$
- (b) **M1** compute entries: first $= \cos 72 * 0 + (-\sin 72) * r = -r \sin 72$; second $= \sin 72 * 0 + \cos 72 * r = r \cos 72$
- (b) **A1** state $W = (-r \sin 72, r \cos 72)$ cao
- (b) **Answer: $W = (-r \sin 72, r \cos 72)$**